

Estimation of the degree of agreement of empirical random vectors using central moment functions

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A methodology for estimating the degree of agreement M of empirical random vectors (RV): $v(k) = (v_0, v_1, \dots, v_l)$ of frequencies v_i ($k=i$) of counts k of registered particles by samples of small volume

$\sum_{i=0}^l v_i = n < 20, 0 \leq v_i \leq n$

and average $\langle k \rangle < 5$ was developed.

The degree of agreement of the vectors is estimated by the test statistics of the closeness of the projections of the fractional order functions $1 < S$ of the central moments $\mu(v(k), S)$ RV- v :

$\mu(v, S) = 1/(n-1) \sum_{i=1}^l (k_i - k) S = \text{Re}(S, \mu(\cdot)) + i \text{Im}(S, \mu(\cdot)), i^2 = -1,$

Where $\text{Re}(\cdot)$ and $\text{Im}(\cdot)$ is real and imaginary components of the central moments function $1 < S$. As a test statistic to estimate the agreement of projections $\mu(S)$ there was proposed a metric

$\Phi = \sum_{S=0}^l S \frac{((\text{Re}(\mu_{(1,g)}) - \text{Re}(\mu_{(1,h)})) / ((\text{Re}(\mu_{(1,g)}) + \text{Re}(\mu_{(1,h)}))) i^2 + ((\text{Im}(\mu_{(1,g)}) - \text{Im}(\mu_{(1,h)})) / ((\text{Im}(\mu_{(1,g)}) + \text{Im}(\mu_{(1,h)}))) i^2}{(S_m - S_0)}$

$\cdot 1/(S_m - S_0)$

The methodology is based on the mutual one-to-one correspondence of the random vector $v(\cdot) = (v_0, v_1, \dots, v_l), \sum_{i=0}^l v_i = n < 20, v_i$ ($k=j$), in the sample and the complex function of fractional order $1 < S_0 < S_m \leq 5$ of central moment of vector $v(\cdot)$.

References

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No

Section

1. Applications of nuclear methods in science and technology

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