

LXXII INTERNATIONAL CONFERENCE  
NUCLEUS – 2022: Fundamental problems and applications

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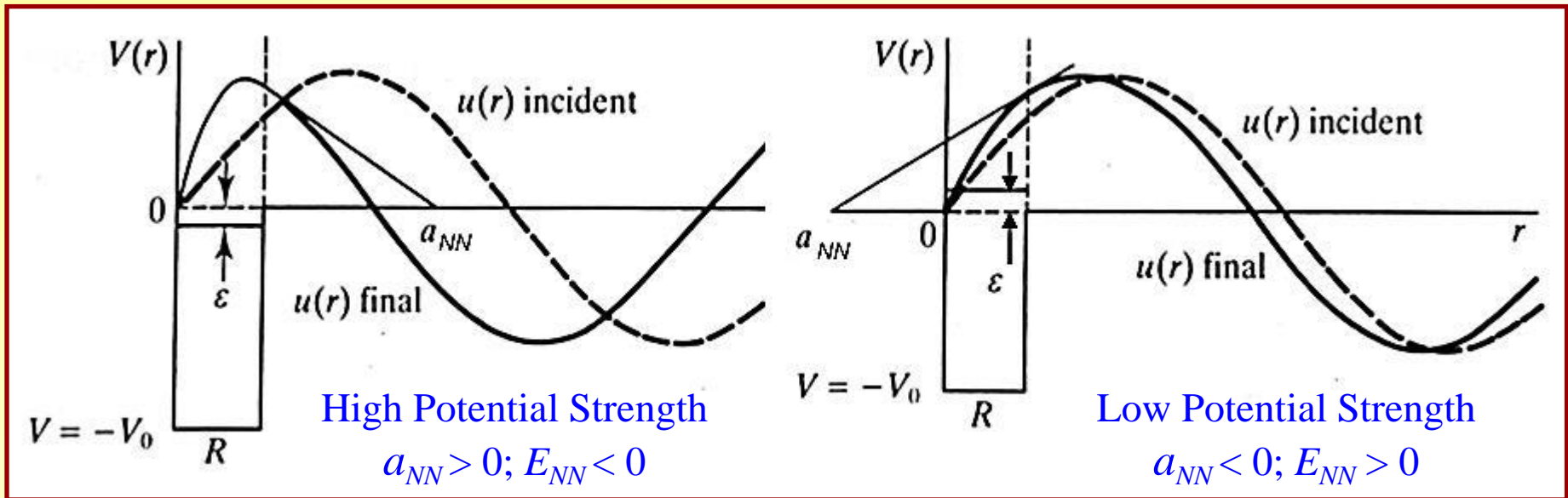
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**DATA ON THE  $np$ -SCATTERING LENGTH FROM  
THE  $nd$ -BREAKUP REACTION AT LOW ENERGIES**

# Low-Energy Parameters of NN-Interaction

NN-Scattering Lengths  $a_{NN}$  and NN-Virtual State Energy  $E_{NN}$

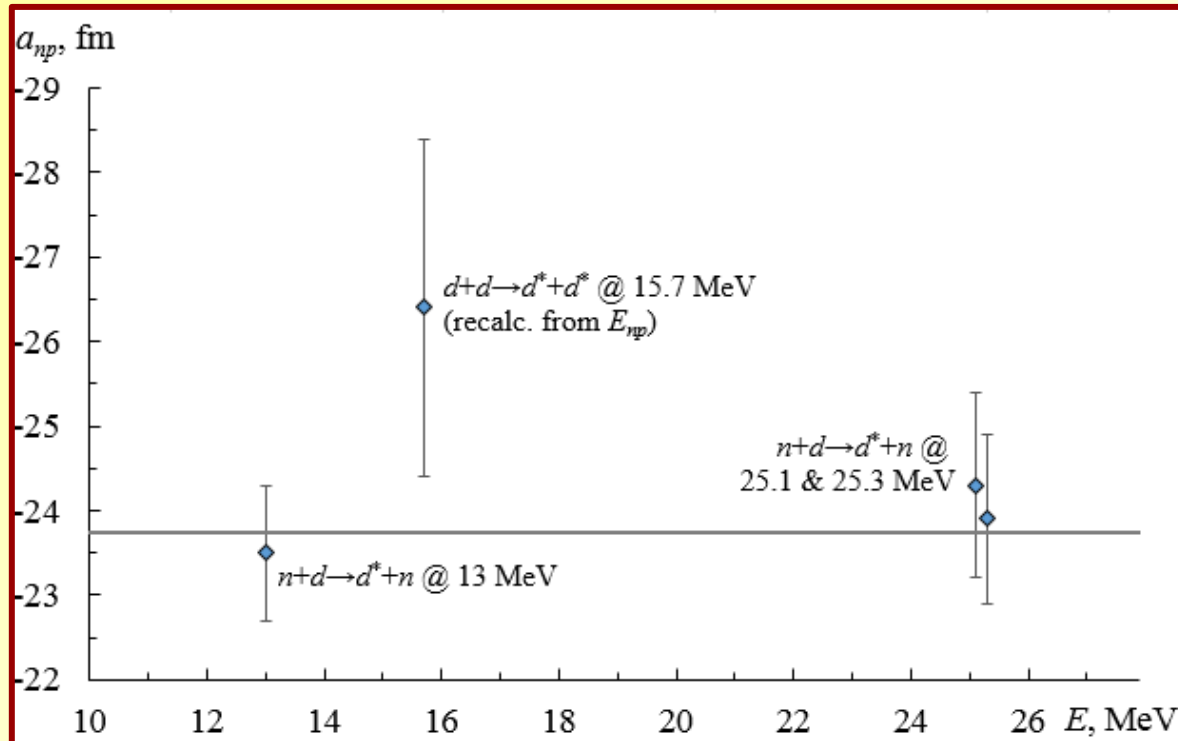
$$\frac{1}{a_{NN}} = -\left(\frac{m_N E_{NN}}{\hbar^2}\right)^{1/2} - \frac{1}{2} r_{NN} \frac{m_N E_{NN}}{\hbar^2} + \dots$$



Scattering length is determined as the intersection point of the tangent at the joining point of the inner and outer WF with the  $R$ -axis.

Small change in potential strength can lead to a significant change in the scattering length.

# Data on Neutron-Proton Scattering Length

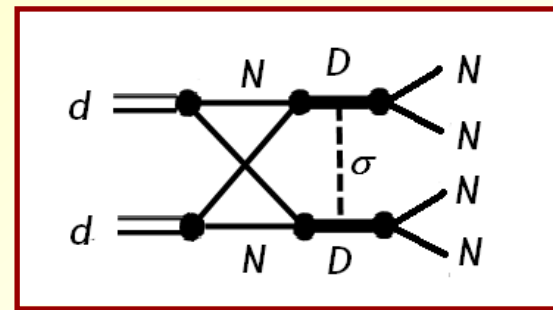
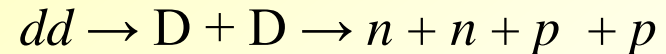
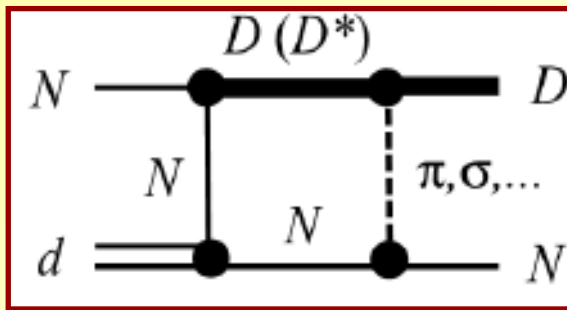
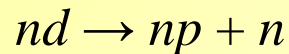


Accurate experimental data on the scattering lengths and their differences may provide a quantitative estimate of the charge symmetry breaking (CSB) and charge independence breaking (CIB) of nuclear forces

$a_{np} = -23.748 \pm 0.010 \text{ fm}$  is determined from direct measurement of the  $np$ -scattering (grey line)

# Dibaryon Model (V.I. Kukulin *et al.*)

New mechanism arising in the Dibaryon Model: New force – meson exchange between the nucleon and dibaryon



Such additional interaction can lead to a change in the values of  $a_{np}$  and  $E_{np}$ .

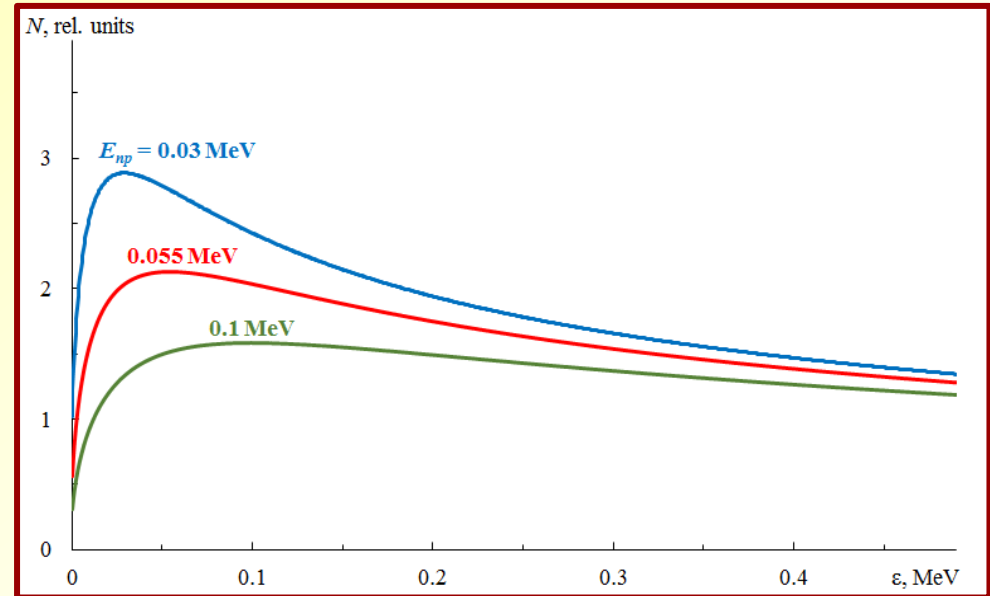
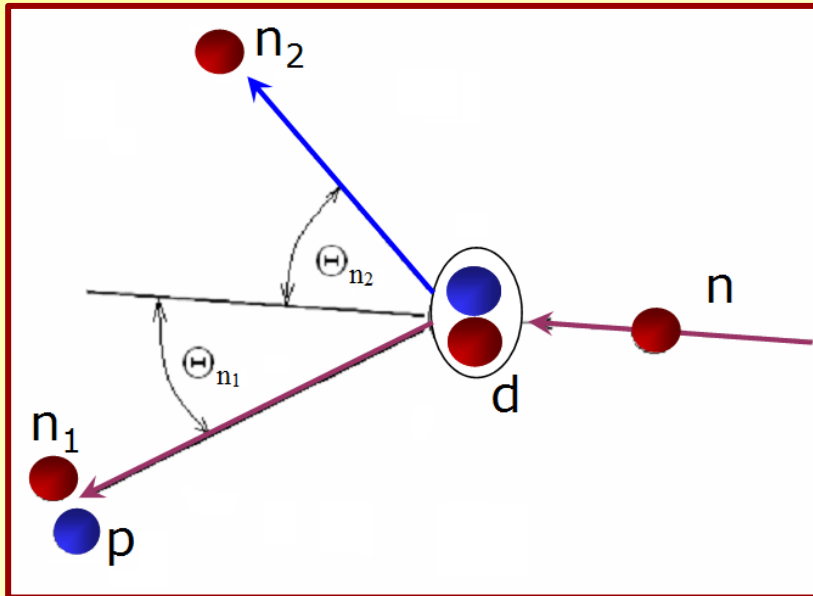
The degree of this change may depend on the relative velocity of the fragments -  $np$ -pair and  $n$  or  $np$ -pair and diproton for  $nd$ - and  $dd$ -breakup, respectively.

# Study of neutron–proton final state interaction (FSI) in $n + d \rightarrow p + n + n$ reaction (*recoil geometry*)

Registration of two neutrons, neutron and proton have a very small relative momentum

Watson-Migdal approximation

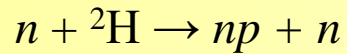
$$\frac{dN}{d\varepsilon}{}_{WM} = \frac{\sqrt{\varepsilon}}{\varepsilon + E_{np}}$$



Neutron–proton FSI manifests itself as a peak in the dependence of the reaction yield on the relative energy of two neutrons  $\varepsilon = \frac{1}{2} \cdot (E_1 + E_2 - 2 \cdot \sqrt{E_1 \cdot E_2} \cdot \cos \Delta\Theta)$   
 The shape of this dependence  $N(\varepsilon)$  is sensitive to  $E_{np}$  and  $a_{np}$ , accordingly.

# Simulation of $nd$ -Breakup Yield vs $\varepsilon$ @ 8–13 MeV

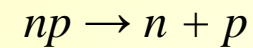
First stage



$$M_{np} = m_n + m_p + \varepsilon$$

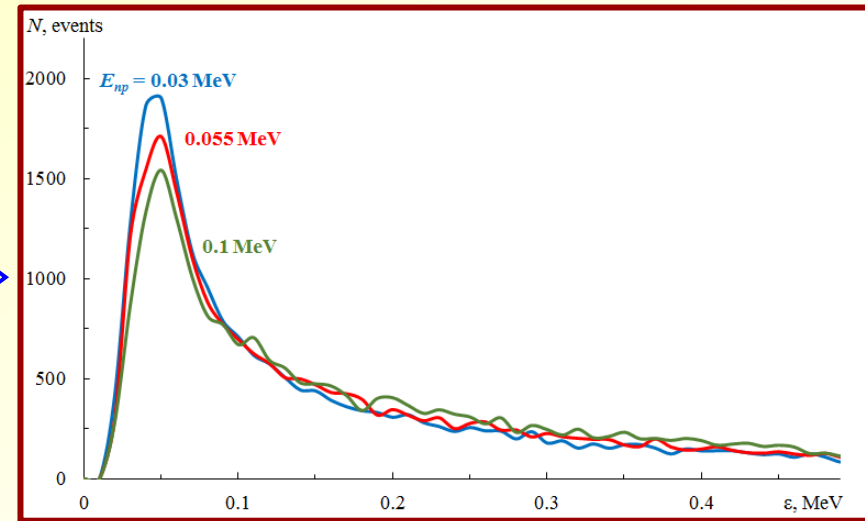
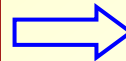
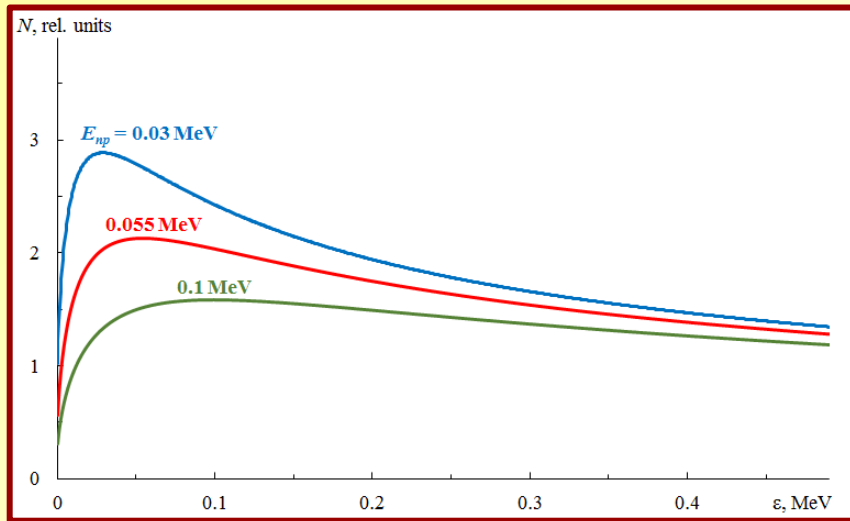
$$N(\varepsilon) - \text{MW}$$

Second stage



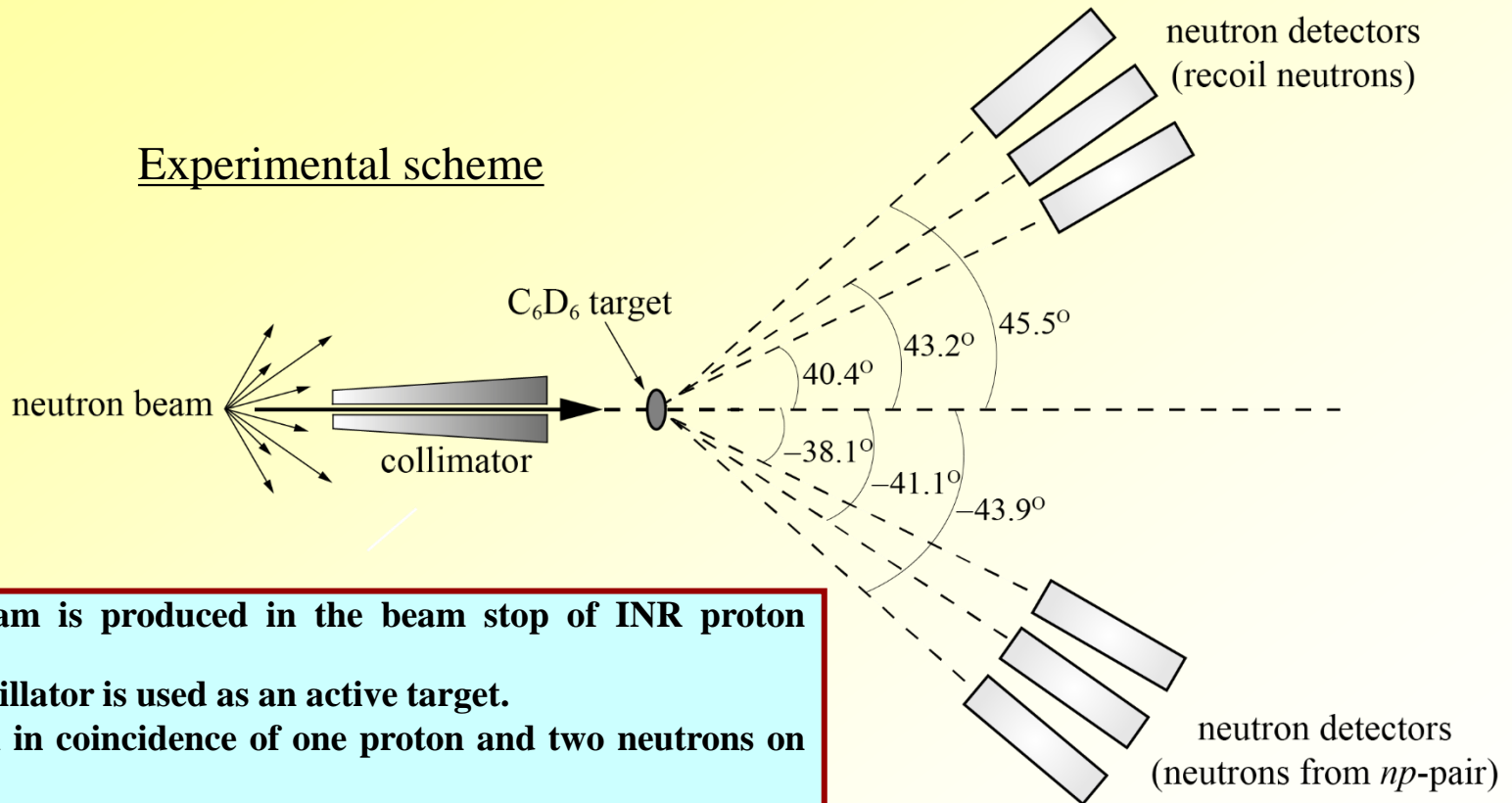
Experimental conditions

$$N(\varepsilon) = f(E_{np})$$



Simulated distribution of the reaction yield on the relative energy depends on  $E_{np}$  ( $a_{np}$ )

# Determination of $E_{np}$ and $a_{np}$ in $n + {}^2\text{H} \rightarrow n + n + p$ reaction at $E_n = 8 - 13$ MeV



- Neutron beam is produced in the beam stop of INR proton accelerator
- A  $\text{C}_6\text{D}_6$  scintillator is used as an active target.
- Registration in coincidence of one proton and two neutrons on opposite sides
- Neutrons are detected by scintillators with  $n\gamma$ -separation
- Energy and angle of the proton are recovered from the conservation laws
- The dependence of  $nd$ -breakup yield on  $np$ -relative energy were compared with MW calculation depending on  $E_{np}$  value

# Experiment vs Simulation.

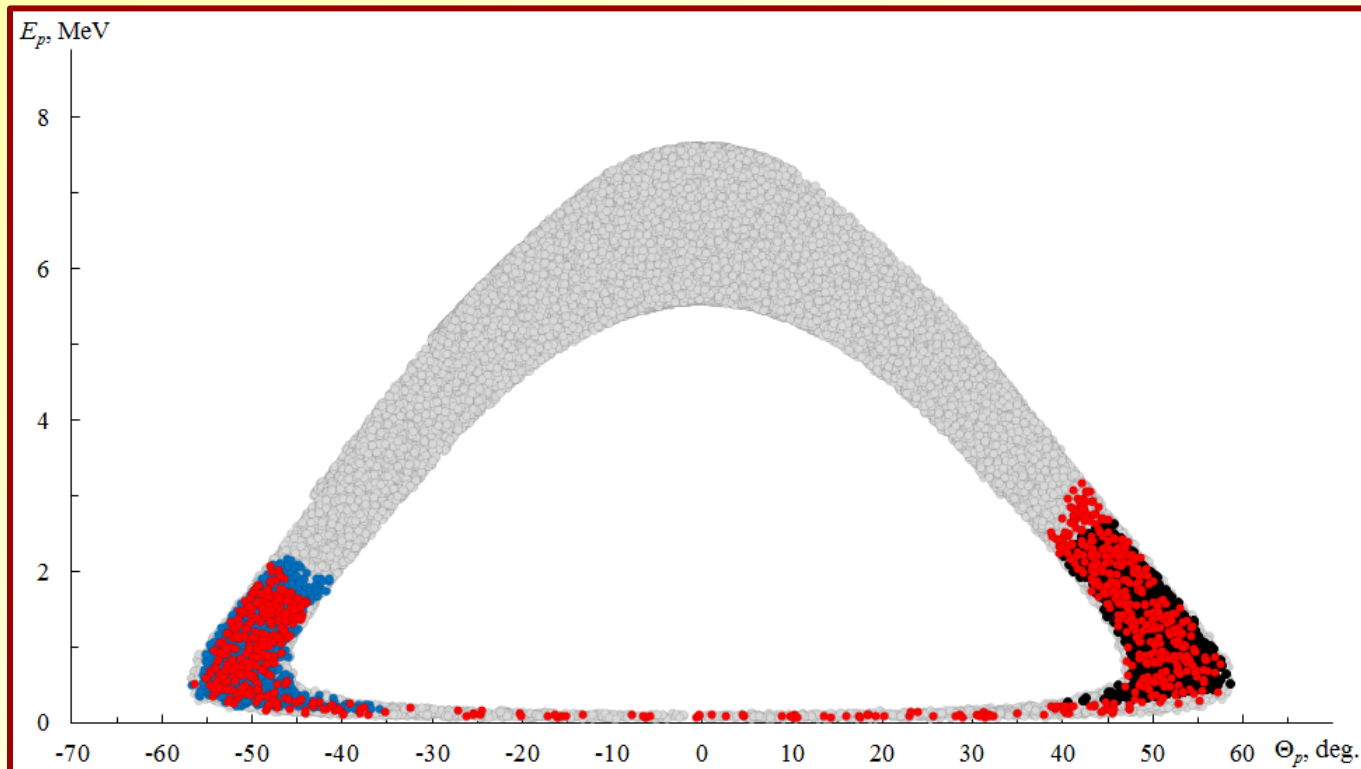
$$E_0 = 9 \pm 1 \text{ MeV}; \Theta_{n1} = -38.07^\circ \pm 0.83^\circ; \Theta_{n2} = 45.47^\circ \pm 0.78^\circ$$

Grey area – simulation  $n + {}^2\text{H} \rightarrow n_1 + p + n_2$  reaction (democratic breakup);

Black area – simulation  $n + {}^2\text{H} \rightarrow (n_1p) + n_2 \rightarrow n_1 + p + n_2$  reaction (intermediate state);

Blue area – simulation  $n + {}^2\text{H} \rightarrow (n_2p) + n_1 \rightarrow n_2 + p + n_1$  reaction (intermediate state);

Red area – experiment

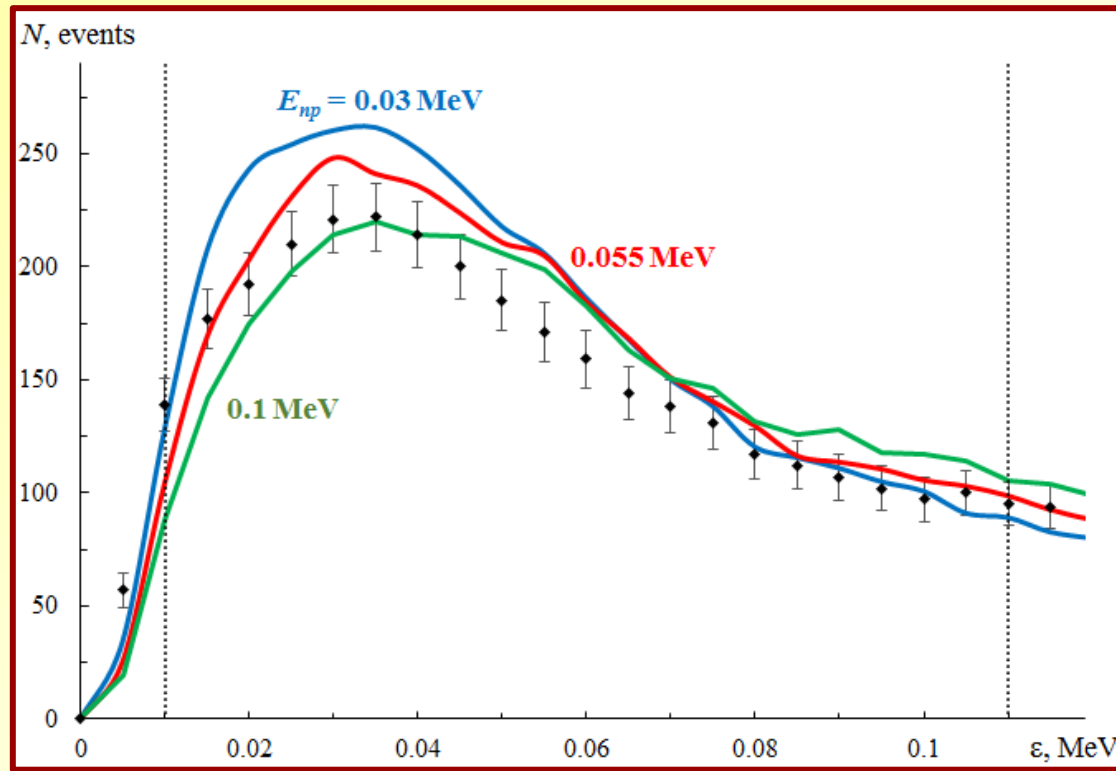




# Experiment vs Simulation.

$$E_0 = 9 \pm 1 \text{ MeV}$$

Total experimental dependence of the yield is compared with the simulation results for three values of np virtual energy 30, 55, and 100 keV.



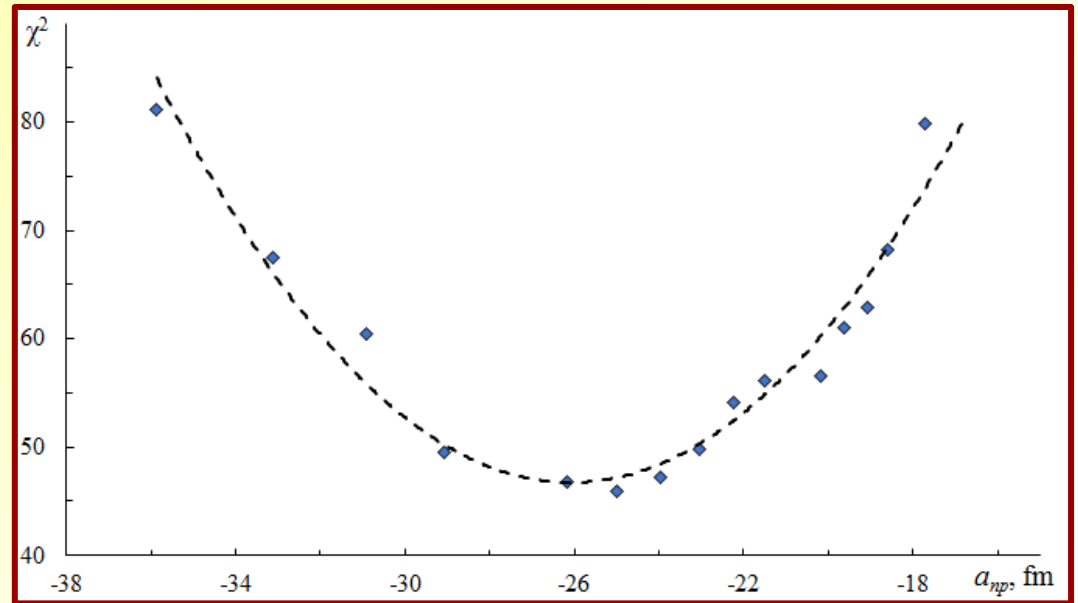
The best fit is obtained for  $E_{np} = 56 \pm 5 \text{ keV}$

# Determination of $E_{np}$ from $\chi^2$ versus $a_{np}$ curve for $E_0 = 9 \pm 1$ MeV and $E_0 = 11 \pm 1$ MeV

Comparing experimental yield with simulation results for different  $a_{np}$

$$\chi^2(a_{np}) = \sum_{\varepsilon} \frac{\left( \frac{dN^{\text{exp}}(\Delta\Theta)}{d\varepsilon} - A \frac{dN^{\text{sim}}(\Delta\Theta)}{d\varepsilon} \right)^2}{\left( \Delta \frac{dN^{\text{exp}}(\Delta\Theta)}{d\varepsilon} \right)^2}$$

Summed over 21 points  $\varepsilon = 0.01 - 0.11$



$$\frac{1}{a_{NN}} = - \left( \frac{m_N E_{NN}}{\hbar^2} \right)^{1/2} - \frac{1}{2} r_{NN} \frac{m_N E_{NN}}{\hbar^2} + \dots$$

$r_{np} = 2.76$  fm

**Output data at 9 MeV**

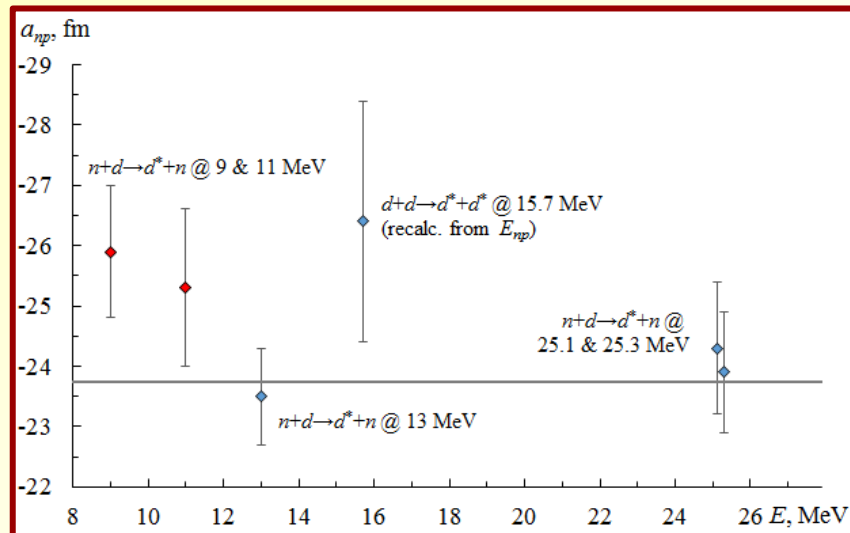
$$a_{np} = -25.9 \pm 1.1 \text{ fm (Recalc. from } E_{np}\text{)}$$

**Output data at 11 MeV**

$$a_{np} = -25.1 \pm 1.3 \text{ fm (Recalc. from } E_{np}\text{)}$$

# Conclusions

- A kinematically complete  $nd$ -breakup experiment at neutron energies 9 and 11 MeV was performed at neutron channel RADEX of INR RAS.
- The shape analysis of the dependence of reaction yield on  $np$  relative energy allows to determine Low Energy Parameters of  $np$ -interaction:  $a_{nn} = -25.9 \pm 1.1$  fm and  $a_{np} = -25.1 \pm 1.2$  fm at 9 and 11 MeV, respectively.
- The obtained value of the  $np$ -scattering length differs significantly from the value obtained in direct  $np$ -scattering and, in our opinion, indicates an effective enhancement of the  $np$ -interaction in the presence of a third nucleon (can be associated with a significant influence of  $3N$ -forces).



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**Thank you!**

